



جامعة تكريت
كلية التربية للبنات
قسم الرياضيات
المرحلة الثانية
مادة التفاضل المتقدم

رسم المنحني على شكل زهرة في الاحداثيات القطبية

Graphing flower-shaped curves in Polar Coordinates

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Ex: Sketch the following:

1) $r^2 = 8 \cos(2\theta)$

2) $r^2 = -9 \cos(2\theta)$

3) $r^2 = -16 \sin(2\theta)$

Sol: Let α the angle od around, then

1) $r^2 = 8 \cos(2\theta)$, then $a^2 = 8$,

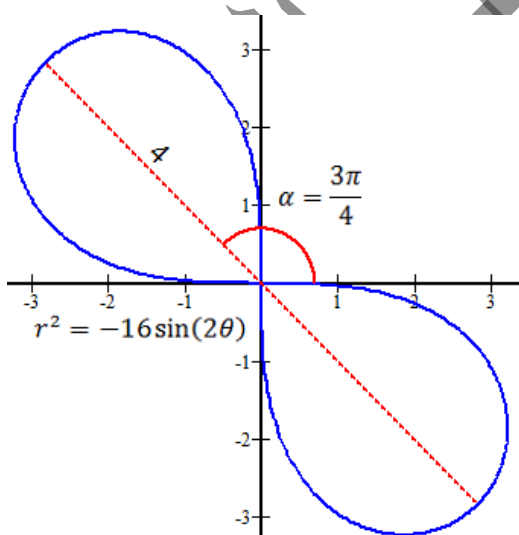
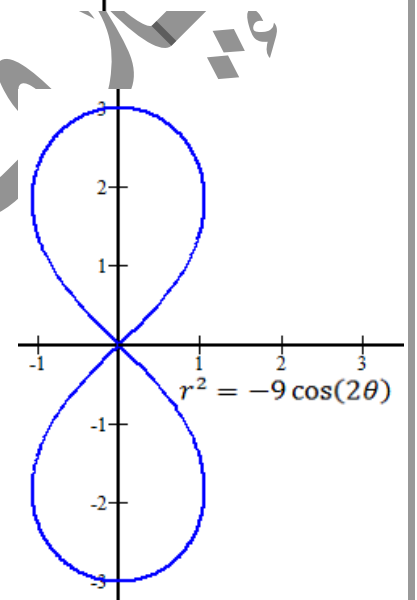
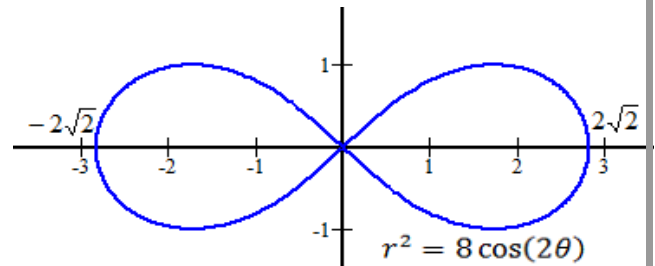
so $a = 2\sqrt{2}$. $\alpha = 0$.

2) $r^2 = -9 \cos(2\theta)$, then $-a^2 = -9$, so $a = 3$.

Or $r^2 = 9 \cos 2 \left(\theta - \frac{\pi}{2} \right)$. $\alpha = \frac{\pi}{2}$.

3) $r^2 = -16 \sin(2\theta)$, then $-a^2 = -16$, so $a = 4$. Or

$r^2 = -16 \cos 2 \left(\theta - \frac{3\pi}{4} \right)$. Therefore $r^2 = 16 \cos 2 \left(\theta - \frac{3\pi}{4} \right)$. $\alpha = \frac{3\pi}{4}$.



Ex: Sketch the following:

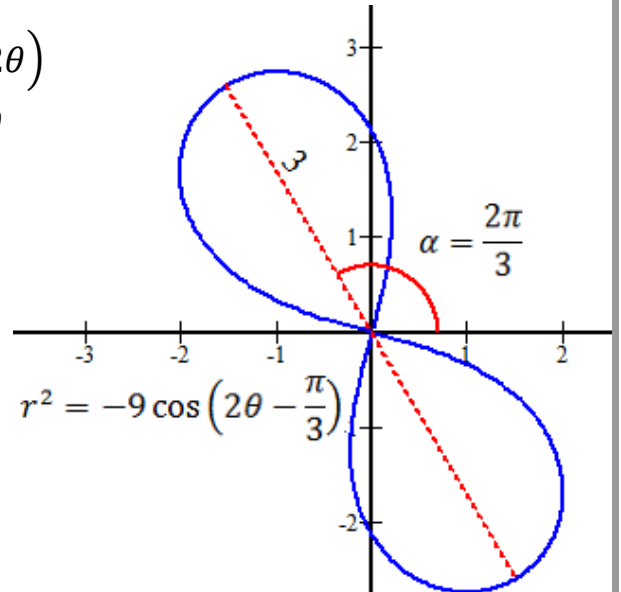
1) $r^2 = -9 \cos\left(2\theta - \frac{\pi}{3}\right)$ 2) $r^2 = 16 \cos\left(\frac{\pi}{4} - 2\theta\right)$
 3) $r^2 = 8 \cos^2 \theta - 4$ 4) $r^2 = 9 - 18 \sin^2 \theta$

Sol: 1) $r^2 = -9 \cos\left(2\theta - \frac{\pi}{3}\right)$

$\Rightarrow r^2 = -9 \cos 2\left(\theta - \frac{\pi}{6}\right)$

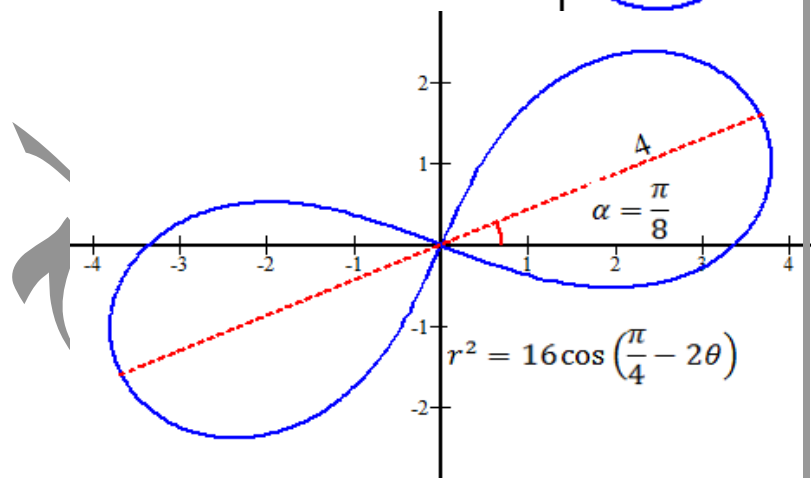
$\Rightarrow r^2 = 9 \cos 2\left(\theta - \frac{2\pi}{3}\right)$

So $\alpha = \frac{2\pi}{3}$.



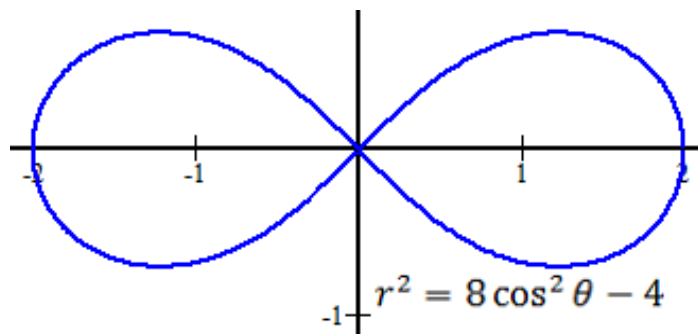
2) $r^2 = 16 \cos\left(\frac{\pi}{4} - 2\theta\right)$

$\Rightarrow r^2 = 16 \cos 2\left(\theta - \frac{\pi}{8}\right)$. $\alpha = \frac{\pi}{8}$.



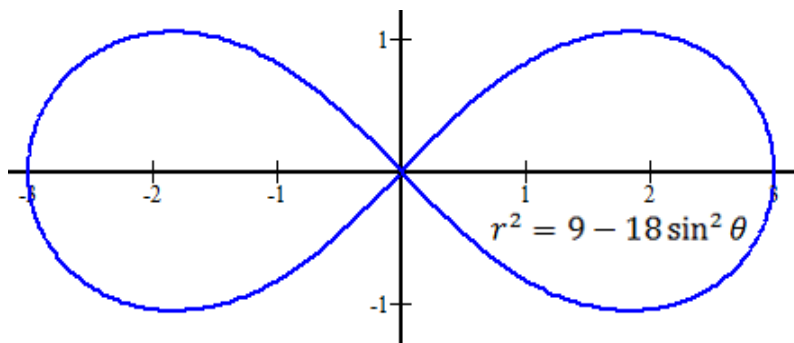
3) $r^2 = 8 \cos^2 \theta - 4$

$\Rightarrow r^2 = 4(2 \cos^2 \theta - 1) = 4 \cos(2\theta)$.



$$4) r^2 = 9 - 18 \sin^2 \theta$$

$$\Rightarrow r^2 = 9(1 - 2 \sin^2 \theta) = 9 \cos(2\theta).$$



Ex: Sketch the following: (H.W.)

$$1) r^2 = \pm a^2 \sin \theta \quad 2) r^2 = \pm a^2 \cos \theta \quad 3) r^2 = 9 \cos \left(\theta + \frac{\pi}{6} \right).$$

(4) Rose Curve

Equations of the form

$$r = a \sin(n\theta) \quad n > 1, n \in \mathbb{Z}^+$$

$$r = a \cos(n\theta) \quad n > 1, n \in \mathbb{Z}^+$$

Represent **flower-shaped** curves called **Roses**

Remark:

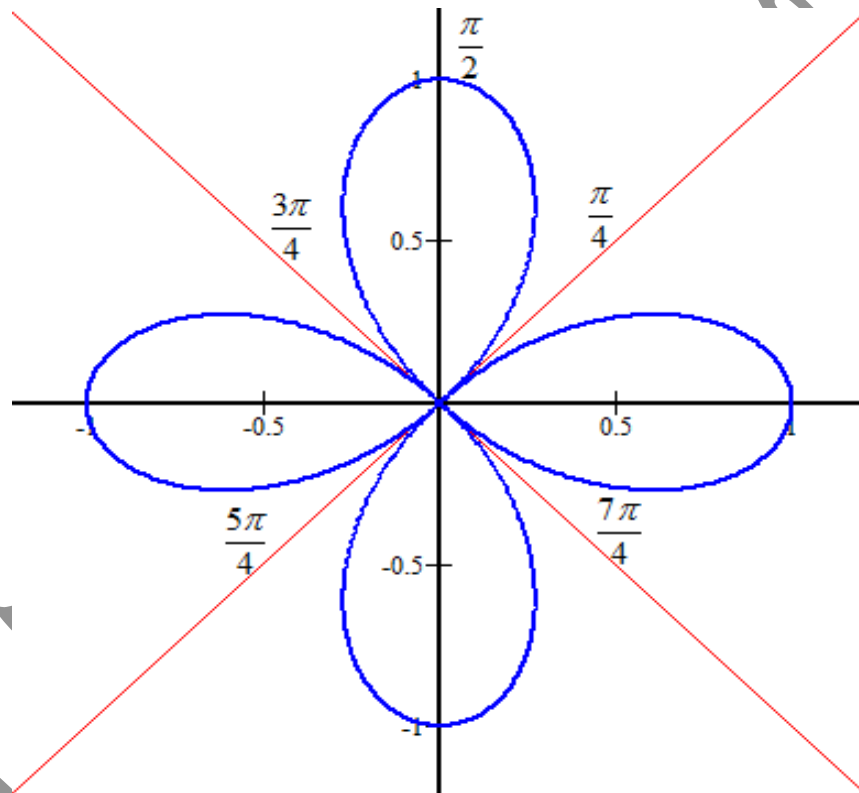
- ❖ يكون رسم وردة ذات (n) ورقة اذا كان عدداً فردياً.
- ❖ يكون رسم وردة ذات (2n) ورقة اذا كان عدداً زوجياً.

Ex: Sketch $r = \cos 2\theta$

Sol: when $r = 0 \Rightarrow \cos 2\theta = 0 \Rightarrow 2\theta = \frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, \dots \Rightarrow \theta = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \dots$

So $r = 1 \Rightarrow \cos 2\theta = 1 \Rightarrow 2\theta = 0, \frac{4\pi}{2}, \frac{8\pi}{2}, \frac{12\pi}{2}, \dots \Rightarrow \theta = 0, \pi, 2\pi, 3\pi, \dots$

also $r = -1 \Rightarrow \cos 2\theta = -1 \Rightarrow 2\theta = \frac{2\pi}{2}, \frac{6\pi}{2}, \frac{10\pi}{2}, \dots \Rightarrow \theta = \frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, \dots$



Ex: Sketch $r = \sin 3\theta$ 3-leafs

Sol: when $r = 0 \Rightarrow \sin 3\theta = 0 \Rightarrow 3\theta = 0, \frac{2\pi}{2}, \frac{4\pi}{2}, \frac{6\pi}{2}, \dots \Rightarrow \theta = 0, \frac{\pi}{3}, \frac{2\pi}{3}, \pi, \dots$

So $r = 1 \Rightarrow \sin 3\theta = 1 \Rightarrow 3\theta = \frac{\pi}{2}, \frac{5\pi}{2}, \frac{9\pi}{2}, \dots \Rightarrow \theta = \frac{\pi}{6}, \frac{5\pi}{6}, \frac{9\pi}{6}, \dots$

also $r = -1 \Rightarrow \sin 3\theta = -1 \Rightarrow 3\theta = \frac{3\pi}{2}, \frac{7\pi}{2}, \frac{11\pi}{2}, \dots \Rightarrow \theta = \frac{3\pi}{6}, \frac{7\pi}{6}, \frac{11\pi}{6}, \dots$

